

KVS BHOPAL REGION CBT TEST AUG 2023
SUBJECT-MATHEMATICS
CLASS-11

TOPICS:

SETS, RELATIONS AND FUNCTIONS, TRIGONOMETRY

Case Study – 1

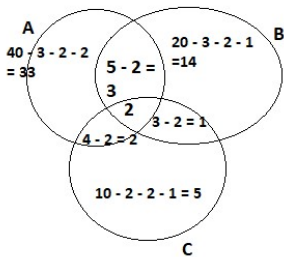
In a small town of 10,000 families, it was found that 40% of the families buy newspaper A, 20% buy newspaper B, 10% buy newspaper C, 5% buy A and B, 3% buy B and C and 4% buy A and C. 2% of the families buy all the three newspapers.

Now answer following questions (Q1 to Q4)

Q1. Find the number of families which buy **newspaper A only**.

(a) 3100 (b) 3200 (c) 3300 (d) 3400

Feedback



The number of families which buy newspaper *A only*

$$= (40 - 3 - 2 - 2)\% \text{ of } 10000$$

$$= \frac{33}{100} \times 10000 = 3300$$

Q2. Find the number of families which buy **exactly two newspapers**.

(a) 200 (b) 600 (c) 800 (d) 1000

Feedback

The number of families which buy **exactly two newspapers**

$$= (3 + 2 + 1)\% \text{ of } 10000$$

$$= \frac{6}{100} \times 10000 = 600$$

Q3. Find the number of families which buy **none of the newspapers A, B and C**.

(a) 6000 (b) 4400 (c) 4200 (d) 4000

Feedback

The number of families which buy **none of the newspapers A, B and C**
 $= (100 - 33 - 14 - 5 - 3 - 2 - 2 - 1)\% \text{ of } 10000$
 $= (100 - 60)\% \text{ of } 10000$
 $= \frac{40}{100} \times 10000 = 4000$

Q4. Find the number of families which buy **exactly one newspaper**.

(a) 4800 (b) 5200 (c) 6000 (d) 4000

Feedback

The number of families which buy **exactly one newspaper**
 $= (33 + 14 + 5)\% \text{ of } 10000$
 $= \frac{52}{100} \times 10000 = 5200$

Case Study 2

After school hours, Manisha, student of class XI is attending hobby classes and doing a designing course. Now a days she is working on a canvas similar to cartesian plane. For making a particular design she wants to take x-coordinate from the set $A = \{0, 1, 2, 3, 5\}$ and y-coordinate from the set $B = \{-3, -2, -1, 0, 1, 2, 3\}$

Based on the above information answer the following questions (Q5 to Q7)

Q5. How many ordered pairs Manisha can make from A to B ?

(a) 12 (b) 30 (c) 35 (d) 40

Feedback

No. of ordered pair
 $= n(A) \times n(B) = 5 \times 7 = 35$

Q6. If a relation from A To B is defined as $R = \{ (a , b) : a < b, a \in A , b \in B \}$.

Then how many elements are there in R

(a) 6 (b) 8 (c) 12 (d) 20

Feedback

$R = \{(0,1), (0,2), (0,3), (1,2), (1,3), (2,3)\}$
elements are there in R = 6

Q7. How many total relations can be defined from the Set A to the set B?

(a) 2^5 (b) 2^7 (c) 2^{12} (d) 2^{35}

Feedback

$$\text{No. of relations} = 2^{n(A) \times n(B)} = 2^{5 \times 7} = 2^{35}$$

Q8. Assertion (A): If A and B are two sets such that, $n(A) = 3$, $n(B) = 6$ and $A \subset B$, then the number of elements in $A \cup B$ is 9.

Reason (R): If A and B are disjoint sets, then $n(A \cup B)$ is $n(A) + n(B)$.

- (a) A is true, R is true; R is a correct explanation of A.
- (b) A is true, R is true; R is not a correct explanation of A.
- (c) A is true; R is false.
- (d) A is false; R is true.

Feedback

Assertion (A) is false as

$$\because A \subset B$$

$$\therefore A \cup B = B$$

$$\Rightarrow n(A \cup B) = n(B) = 6$$

Reason (R): True

Q9. The value of $\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ$ is

- (a) 0 (b) 1 (c) -1 (d) not defined

Feedback

$$\begin{aligned} & \tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ \\ &= \tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 45^\circ \dots \tan(90^\circ - 3^\circ) \tan(90^\circ - 2^\circ) \tan(90^\circ - 1^\circ) \\ &= \tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 45^\circ \dots \cot 3^\circ \cot 2^\circ \cot 1^\circ \\ &= \tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \times 1 \times \dots \times \frac{1}{\tan 1^\circ} \times \frac{1}{\tan 2^\circ} \times \frac{1}{\tan 3^\circ} = 1 \end{aligned}$$

Q10. What is the value of $\cot(-870^\circ)$?

- (a) $\sqrt{3}$ (b) $1/\sqrt{3}$ (c) $-\sqrt{3}$ (d) $-1/\sqrt{3}$

Feedback

$$\begin{aligned} \cot(-870^\circ) &= -\cot 870^\circ = -\cot(2 \times 360^\circ + 150^\circ) = -\cot 150^\circ \\ &= -\cot(180^\circ - 30^\circ) = -(-\cot 30^\circ) = \sqrt{3} \end{aligned}$$

Answer Key

| | | | | |
|--------------|--------|---|---|---|
| Case Study 1 | c | b | d | b |
| Case Study 2 | c | a | d | d |
| Q9. b | Q10. a | | | |